



LOYOLA COLLEGE (AUTONOMOUS) CHENNAI – 600 034

M.Sc. DEGREE EXAMINATION – STATISTICS

SECOND SEMESTER – APRIL 2025

PST2ME01 – TIME SERIES MODELLING



Date: 07-05-2025

Dept. No.

Max. : 100 Marks

Time: 01:00 PM - 04:00 PM

SECTION A – K1 (CO1)

Answer ALL the questions

(5 x 1 = 5)

1 True or False

- Holt's linear method is also known as Double exponential smoothing.
- In a multiplicative time series model the **seasonal fluctuations** grow or shrink **proportionally** to the level of the trend.
- ACF at lag 1 is equal to PACF at lag 1.
- A autoregressive model is also known as distributed lag model.
- In a ARIMA model with parameters p,d,q the value of q cannot be zero.

SECTION A – K2 (CO1)

Answer ALL the questions

(5 x 1 = 5)

2 Match the following

- Y_{t-k} - Holt Winter
- Order of differencing - no predictable pattern
- Stationarity - d
- Smoothing - Augmented Dickey Fuller test
- White noise - Lag of order k

SECTION B – K3 (CO2)

Answer any THREE of the following

(3 x 10 = 30)

- Discuss any ten real life applications of time series forecasting models.
- (i) Discuss additive model, multiplicative model and its various components.
(ii) Explain Single Exponential Smoothing, Holt's linear method and Holt-Winter's trend and seasonality method of smoothening
- Define Autocorrelation of order 1, order 2, order k and partial autocorrelation of order 1, order 2 and order k and discuss the methods to determine autocorrelation of order k and partial autocorrelation of order k
- Discuss (i) Random Walk model (ii) Random walk with drift (iii) Use of Back-shift notation (3+3+4)
- Discuss Box-Jenkins method of constructing ARIMA model

SECTION C – K4 (CO3)	
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	Answer any TWO of the following	(2 x 12.5 = 25)
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| 8 | Obtain quarterly forecast for the next year using multiplicative model.
Year : 1 1 1 1 2 2 2 2 3 3 3 3 4 4 4 4
Quarter : Q1 Q2 Q3 Q4 Q1 Q2 Q3 Q4 Q1 Q2 Q3 Q4 Q1 Q2 Q3 Q4
Sales : 4.8, 4.1, 6, 6.5, 5.8, 5.2, 6.8, 7.4, 6, 5.6, 7.5, 7.8, 6.3, 5.9, 8, 8.4 |
| 9 | Explain stationary in time series analysis and discuss the test for stationarity of time series data. |
| 10 | Determine auto correlation of order 1 and order 2 based on the following data:
5, 7, 6, 8, 10, 12, 14, 13, 11, 15 |
| 11 | i) Explain Koyck model in detail (10 Marks)

(ii) What is out-of-time model validation in time series? Explain with an example (2.5 Marks) |

SECTION D – K5 (CO4)

	Answer any ONE of the following	(1 x 15 = 15)
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	Answer any ONE of the following	(1 x 15 = 15)
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| 12 | <p>Determine any four model performance measures used in time series based on the data given below</p> <p>Actual Y : 112 98 102 112 87 96 112 101 99 105 123 143</p> <p>Forecasted Y : 106.5 96.5 108 121 81 90 121 95 97 101 132 139</p> |
| 13 | <p>Determine Partial autocorrelation of order 1, order 2 and order 3 for the data given below:</p> <p>Sales: 3, 5, 7, 9, 10, 12</p> |

SECTION E – K6 (CO5)	
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	Answer any ONE of the following	(1 x 20 = 20)
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	Answer any ONE of the following	(1 x 20 = 20)
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|------------|---|-------|------|------|------|------|------|------|------|------|------------|---|---|---|---|---|---|---|---|--------|------|------|----|------|------|------|------|------|
| 14 | <p>Use linear regression with dummy variables and obtain the half-yearly forecast for the year 2025.
 Half_year = 0 indicates Jan-Jun, Half_year = 1 indicates Jul-Dec</p> <table border="1"> <tr> <td>Year:</td><td>2021</td><td>2021</td><td>2022</td><td>2022</td><td>2023</td><td>2023</td><td>2024</td><td>2024</td></tr> <tr> <td>Half_year:</td><td>0</td><td>1</td><td>0</td><td>1</td><td>0</td><td>1</td><td>0</td><td>1</td></tr> <tr> <td>Sales:</td><td>19.9</td><td>22.5</td><td>21</td><td>24.2</td><td>21.6</td><td>25.3</td><td>22.2</td><td>26.4</td></tr> </table> | Year: | 2021 | 2021 | 2022 | 2022 | 2023 | 2023 | 2024 | 2024 | Half_year: | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 | Sales: | 19.9 | 22.5 | 21 | 24.2 | 21.6 | 25.3 | 22.2 | 26.4 |
| Year: | 2021 | 2021 | 2022 | 2022 | 2023 | 2023 | 2024 | 2024 | | | | | | | | | | | | | | | | | | | | |
| Half_year: | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 | | | | | | | | | | | | | | | | | | | | |
| Sales: | 19.9 | 22.5 | 21 | 24.2 | 21.6 | 25.3 | 22.2 | 26.4 | | | | | | | | | | | | | | | | | | | | |
| 15 | <p>i) Discuss the following in detail (a) Auto-regressive Model of order k (b) Moving average model of order k (c) ARMA model (d) ARIMA model and (e) SARIMA model. (15 Marks)</p> <p>ii) Explain how would you determine the optimal p,d,q in ARIMA using Train,Test and Validation datasets. (5 Marks)</p> | | | | | | | | | | | | | | | | | | | | | | | | | | | |